# 1 Direct Measurements and Numerical Predictions of Welding-Induced

# 2 Initial Deformations in a Full-Scale Steel Stiffened Plate Structure

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Myung Su Yi<sup>a</sup>, Dong Hun Lee<sup>a</sup>, Hyun Ho Lee<sup>a</sup> and Jeom Kee Paik<sup>a,b,c\*</sup>

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<sup>a</sup>Department of Naval Architecture and Ocean Engineering, Pusan National
University, Busan, Republic of Korea

- <sup>8</sup> <sup>b</sup>The Korea Ship and Offshore Research Institute (The Lloyd's Register Foundation
- 9 Research Centre of Excellence), Pusan National University, Busan, Republic of Korea
- <sup>10</sup> <sup>c</sup>Department of Mechanical Engineering, University College London, London, UK
- 11 \* Corresponding author. J.K. Paik. Email. j.paik@ucl.ac.uk
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## 13 Abstract

As a sequel to another paper of the authors on welding-induced residual stresses [1], 14 15 this paper aims to obtain a direct measurement database of welding-induced plate initial deflections in a full-scale steel stiffened plate structure and also to study the 16 applicability of computational models to predict them. A full-scale steel stiffened 17 plate structure in association with bottom plate panels of an as-built 1,900 TEU 18 containership is fabricated by exactly the same technology of welding as used in 19 today's shipbuilding industry. The 3D scanner is employed to measure 20 welding-induced initial deformations of the structure. Computational models using the 21 three-dimensional thermo-elastic-plastic finite element method are developed to 22 predict the plate initial deflections. A comparison between direct measurements and 23 numerical predictions is made. Details of direct measurement databases are 24 25 documented as they are useful to validate the computational models formulated by other researchers. 26

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Keywords: Steel stiffened plate structures, welding-induced initial deformations,
full-scale measurements, three-dimensional thermo-elastic-plastic finite element
method, 3D scanner

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# 32 **1. Introduction**

Welding-induced initial deformations are unavoidable in fabrication of steel structures, 33 as shown in Fig. 1, and they significantly affect the buckling and ultimate strength 34 which are primary criteria for structural analysis and design [2,3]. Structural analysis 35 and design need to start with an adequate definition of such initial imperfections. As 36 37 would be expected, the welding-induced initial deformations in thin-walled structures are greater than in thick-walled structures. Thin-walled structures are likely to subject 38 to thermal plate buckling in the process of fabrication, as shown in Fig. 2, resulting in 39 costly fairing works to remove distortions. 40 41



Fig. 1. Typical patterns of welding-induced initial deformations in stiffened plate structures [2].



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**Fig. 2.** Example of welding-induced deformations in thin-walled structures [5].

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A number of studies on this topic are available in the literature, and their survey is 49 found in Ueda [4] and Paik [2], among others. The previous studies include both 50 direct measurements and numerical predictions. A few measurement studies were 51 performed with full-scale structure models [5]. Most of previous studies used 52 53 small-scale models which were far different from the actual welding in practice, which would significantly affect the resulting measured initial deformations in 54 magnitude and pattern. Therefore, the development of direct measurement databases 55 of welding-induced initial deformations in full-scale steel stiffened plate structures is 56

highly demanded. A number of studies in numerical predictions of welding-inducedinitial deflections are also available in the literature [6-13].

The objective of the paper is to contribute to the development of direct measurement databases of welding-induced initial deformations in full-scale steel stiffened plate structures, and also to study the applicability of numerical predictions using the three-dimensional thermo-elastic-plastic finite element method models formulated by the authors [12,13]. This paper is a sequel to another article of the same authors on welding-induced residual stresses of a full-scale steel stiffened plate structure which is an identical structure used in the present paper [1].

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# 67 2. Design of a full-scale steel stiffened plate structure model

In this paper, plate panels in bottom structures of an as-built containership carrying 1,900 TEU were chosen as the reference vessel, as shown in Fig. 3. Note that containerships in full load condition are in hogging and thus bottom plate panels are subjected to axial compressive loads [3,14,15].

Details of the scantlings for the test structure made of high tensile steel with grade AH32 are provided in Paik et al. [16], and a summary of the structural design is presented here. Fig. 4 shows the geometric properties the structure model which has T-type of longitudinal stiffeners and transverse frames as shown in Fig. 5. With the nomenclature of dimensions for longitudinal stiffeners and transverse frames, their geometric properties are provided in Table 1. The thickness of plating is 10 mm and the structure weighs 4.814 tons.

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Fig. 3. Plate panels in bottom structures of an as-built 1,900 TEU containership.





Fig. 4. Drawing of the full-scale steel stiffened plate structure.



86

87 (a) Longitudinal stiffener (b) Transverse frame
88 Fig. 5. Nomenclature of dimensions.

### 90 **Table 1.** Dimensions of the structure model.

F	Plate proper	ties	Stiffener / Frame properties						
Length,	Breadth,	Thickness,				t	h	t	
а	b	t (mm)	Туре		$n_w$	<sup><i>u</i></sup> <sub>w</sub>	$\nu_f$	$\iota_f$	
(mm)	(mm)	$\iota_p$ (IIIII)			(mm)	(mm)	(mm)	(mm)	
		10	Stiffener	Center	290	10	90	10	
3,150	720		(T-bar type)	Both side	290	20	90	10	
			Frame (T-bar type)	-	665	10	150	10	

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#### 92 **3. Fabrication of the structure model**

The structure is made of high tensile steel with grade AH32. After the material procurement, tensile coupon test specimens were extracted from the steel sheet as per ASTM E8 [17], as shown in Fig. 6(a). The universal test machine together with an extensometer was used for the tension tests as shown in Fig. 6(b). The failure pattern of the tensile coupon specimens was similar, as shown in Fig. 6(c). Fig. 7 shows one of typical engineering stress-engineering strain curves of the material obtained from 99 tensile coupon tests with multiple specimens. Table 2 provides the mechanical100 properties of material AH32.



#### 

(a) Dimension of the tensile test specimen





(b) Specimen with extensometer (c) Specimen after completing tensile test
Fig. 6. Specimen of material used for the structure before and after tensile coupon
tests.



Fig. 7. Engineering stress versus engineering strain curve of material AH32. 110

# 111

**Table 2.** Mechanical properties of material AH32 used for the structure model.
 112

	Grade	E (GPa)	$\sigma_{_{Y}}$ (MPa)	$\sigma_{T}$ (MPa)	V	$\mathcal{E}_{f}$ (%)
	AH32	205.8	331	483	0.3	40.0
113 -						

Note: E is the elastic modulus,  $\sigma_{\gamma}$  is the yield strength,  $\sigma_{\tau}$  is the ultimate tensile 114

strength,  $\nu$  is the assumed Poisson's ratio, and  $\varepsilon_f$  is the fracture strain. 115

116

Table 3. Welding parameters of the actual welding process and welding procedure 117 specifications 118

	Welding parameter								
$L_w$ (mm)		Current	Voltage	Speed	Heat input (KJ/cm)				
_		(A)	(V)	(cm/min)					
-	WPS	225-275	23-32	24-34	7-18				
	Real 260 condition		28	30	14.56				

119

120

The structure was fabricated in a shipyard in Busan, South Korea which builds 121 small and medium sized merchant and patrol ships. The technology of welding was 122 exactly the same as used for fabrication of real ship structures. The steel sheet was 123 procured with one big plate to avoid butt welds to connect multiple pieces of plates. 124 Support members (longitudinal stiffeners or transverse frames) are attached by fillet 125 welds as per the welding requirements of DNVGL [18]. The flux-cored arc welding 126

127 (FCAW) technique was applied in accordance with the welding procedure128 specification (WPS) requirements as indicated in Table 3.

129 It is important to ensure whether the welding has been successful with full 130 penetration of weld materials along weld lines. Fig. 8 confirms that the penetration of 131 welding was fully achieved with a leg length of 7 mm. Fig. 9 shows photos of the 132 structure after fabrication was completed in the shipyard.

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134 135 136

Fig. 8. Full penetration of welds with a leg length of 7 mmm.



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Fig. 9. The structure after completing of fabrication in the shipyard.

#### 140 4. Measuring methods of initial deformations

Three kinds of welding-induced initial deformations are relevant in stiffened plate
panels, namely plate initial deflection, stiffener's deflection and sideways deformation.
Appendix presents all of the three types of measured databases, but this section
focuses on the measurements of plate initial deflection.

A 3D scanner as a non-contact method is employed to measure the 145 welding-induced initial deformations. Table 4 provides the specifications of the 3D 146 scanner used for the measurements. Details of the measuring methods using the 3D 147 scanner may be referred to in Yi et al. [5]. Fig. 10 presents selective photos showing 148 the measurements of initial deformations. As shown in Fig. 11, the measured data is 149 150 automatically recorded by a personal computer in a digital form which can be easily converted for computational modeling. The measuring time was about 20 min. 151 Appendix presents the details of measured databases in a tabulated form which can be 152 used to validate computational models for predicting welding-induced initial 153 deformations. Also, the measured databases are compared with numerical 154 computations in the next section. 155

- 156
- **Table 4.** Details of the 3D scanner used for the measurements.



Measuring instrument : MetraSCAN750 <sup>TM</sup>							
Accuracy	Up to 0.030 mm						
Resolution	0.050 mm						
Measurement rate	480,000 measurements/s						
Accurate measurement of part ranging	0.2 - 10 m						
Operating temperature	5 – 40 °C						

158 159





- 161 Fig. 10. Photos showing the measurements of the welding-induced initial162 deformations using 3D scanner
- 163



(a) Initiation of measuring points



(b) Acquisition of scanned images





(c) Creating a space with scanned data





Fig. 11. Process of measuring welding-induced initial deformations

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#### 166 5. Computational models using the thermo-elastic-plastic finite element method

167 The shape of welding-induced initial deformations in plate panels is very complex [4]. 168 Thinner plate panels may show more complex patterns of initial deformations. The 169 shape of welding-induced initial deformations in plate panels is often modeled as a 170 combination of multiple sinusoidal waves [2,4,5], but an accurate prediction is 171 sometimes required unless direct measurements are realistic.

In this paper, computational models are developed to predict welding-induced initial deformations of plate panels using three-dimensional thermo-elastic-plastic finite element method [12,13] and compared with measured data. As details of the computational modeling techniques are referred to in Seo et al. [12] and Yi et al. [13], only a brief description is made in this paper.

The computational modeling was created in three steps, as shown in Fig. 12. Step I performs a pre-initial deflection analysis where the strain-as-direct-boundary (SDB) technique is applied, which is recognized as one of simplified methods to predict welding-induced initial deformations [19,20]. In Step II, welding induced shrinkage forces (S.F.) are estimated from the relationship with effective heat (Q') input as shown in Fig. 13 [12,21]. In Step III, thermal buckling is analyzed with the pre-initial

# 183 deflections and the shrinkage forces determined in Step II. All of the computations

184 follow the thermo-elastic-plastic finite element method.

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Step I. Pre-initial deflection analysis using SDB method								
Pre- processing	1) Modeling: Geometry and mesh generations2) Material properties: Thermal and mechanical properties of base and filler metals3) Boundary condition: Imaginary heat, Convection and supporting conditions							
Analysis	1) Performing non-linear thermal-mechanical analysis							
Post- processing	<ol> <li>Checking results of global deformation</li> <li>Rezoning mesh</li> <li>Extracting geometry and mesh information from results of Step I</li> </ol>							

Step II. Calculating Shrinkage Force (S.F.)

Calculating from developed empirical formulae (Regression of Q' vs. S.F.)

Step III. Thermal buckling analysis using Arc-length method								
Pre- processing	1) Modeling: Importing from results of Step I2) Material properties: Mechanical properties of base and filler metals3) Boundary condition: Shrinkage force, Supporting conditions							
Analysis	1 ) Performing non-linear mechanical analysis							
Post- processing	1 ) Checking results of global deformation 2 ) Confirming results							

- 187 Fig. 12. Procedure for predicting welding-induced initial deflections in plate panels
- 188 [12,13]
- 189

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**Fig. 13.** Relationship between the shrinkage force versus the effective heat [12].

In the present study, the strain-hardening effects of material are not taken into 193 account, while the mechanical properties of material as indicated in Table 2 are used. 194 The geometry of plate panels is modelled by rectangular type plate-shell finite 195 elements, where the gradient of temperatures over the cross section in the plate 196 thickness direction is approximately distributed. 197

198 The analysis of Step I reveals initial irregularities in the shape of plate panels, where spring elements are used with self-weight at the four vertices of the analysis 199 model. All the six degrees of freedom at the nodes of these spring elements are 200 constrained to prevent rigid body motion. To simulate the situation of an actual 201 welding process, the contact analysis with structural elements is performed in 202 un-deformed state. A contact-friction model is applied using a stick-slip modeling 203 technique for efficient convergence. Fig. 14 presents the boundary conditions of the 204 205 computational models where a symmetric condition is applied along all the four edges of plate panels. This condition is in fact not directly equivalent to the test structure 206 which is a stand-alone plate panel, but it was adopted because real plate panels are 207 arranged continuously in the middle of plated structures. Thermal loads in terms of 208 209 temperatures at top and bottom surfaces of plating are obtained from the analyses of Steps I and II as indicated in Table 5 and they are then applied to individual finite 210 elements along each welding line. 211 212

▶ Initial imperfection analysis ŤУ 6DOF (Pre-welding analysis) 6DOF b Gravity b b 6DOF а а 6DOF а Surface Meshed model : Spring (Rigid surface for contact) (Deformable body for contact) element

(a) Modelling for Step I analysis (prediction of initial irregularities)

- 214
- 215

4	Y ► Thermal buckling analysis A Provide the second sec									
5		$u = [0 \ 0 \ 1]$	$u = [0 \ 0 \ 1]$							
5	$Rot = [0 \ 1 \ 1]$	• u = [1 1 0]	Rot = [0 1 1]							
5		u = [0 0 1]	u = [0 0 1]							
	a	a Rot =	[1 0 1] a							

216

(b) Boundary condition for Step III analysis (thermal buckling analysis)
Fig. 14. Computational modelling for prediction of welding-induced initial deformations in the test structure.

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221	Table 5. Shrinkage	forces and temperatures	obtained from Steps 1	and II.
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$t_p (\mathrm{mm})$	$L_w$ (mm)	S.F. (N)	Imaginary Temp. top, $T_{top}({}^\circ\!\mathbb{C})$	Imaginary Temp. bottom, $T_{bot}$ (°C)	
10	7	31,861.09	0.174	-0.174	

222 Note.  $t_p$  = thickness of plating,  $L_w$  = leg length of welding,  $T_{top}$  = temperature at

top surface of plating,  $T_{bot}$  = temperature at bottom surface of plating.

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#### 225 6. Results and Discussions

Fig. 15 presents the results of computational predictions for welding-induced initial deflections in the structure. Fig. 15 compares the direct measurements and numerical computations of plate initial deflections at cross sections A-A' and B-B' of the test structure.

It is seen from Fig.s 15 and 16 that plate initial deflections happened to one side, 230 i.e., support member side of the structure. Not only plating but also transverse frames 231 deflected by welding. During fabrication, four edges of the structure were left free 232 without constraints. The resulting distortions are small along the short edges of the 233 structure. However, the long edges of the structure were distorted unsymmetrically. 234 The welding-induced initial deflections of plating between transverse frames shows 235 the shape of so-called hungry horse's back, and may be modeled as a combination of 236 multiple sinusoidal waves [2]. 237 238



(a) Results of step I analysis.



Fig. 15. Results of the computational predictions.



(a) Welding-induced initial deflection of plating in the plate length direction.



(b) Welding-induced initial deflection of plating in the plate breadth direction.
Fig. 16. Comparison between direct measurements and numerical computations of plate initial deflections in the test structure.

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Fig. 17 shows the statistical error assessment between direct measurements and numerical computations in plate initial deflection. The mean value and standard deviation are 1.087 and 0.198, respectively in the plate length direction, and 0.890 and 0.391, respectively in the plate breadth direction.



258 (b)

Fig. 17. Statistical analysis of the plate initial deflection: (a) plate length direction, (b)plate breadth direction.

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Ship classification societies or other regulatory bodies specify construction tolerances for strength members as related to the maximum initial deflections with the intention that the initial deformations in the fabricated structure must be less than the corresponding specified values [2]. Some examples of the limit for the maximum plate initial deflections are as follows:

267	
268	NORSOK [22]
269	$\frac{w_{o\max}}{b} \le 0.01$
270	
271	Japanese shipbuilding quality standards [23]
272	$w_{o\max} \leq \begin{cases} 7 mm \text{ for ship bottom plate} \\ 6 mm \text{ for ship deck plate} \end{cases}$
273	where $w_{omax}$ is the maximum or limit of the plate initial deflection, and t is the
274	plate thickness.
275	When the above equations of tolerance are applied to the test structure of this
276	study, the following checks can be made.
277	In the plate length direction ( $w_{omax} = 3.80 \text{ mm}$ ),
278	$\frac{w_{o\max}}{b} = \frac{3.80}{720} = 0.0053 \le 0.01$
279	$w_{o\max} = 3.80 \text{ mm} \leq \begin{cases} 7 \text{ mm for ship bottom plate} \\ 6 \text{ mm for ship deck plate} \end{cases}$

In the plate breadth direction (
$$w_{omax} = 6.17$$
 mm),

$$\frac{w_{o\max}}{b} = \frac{6.17}{720} = 0.0086 \le 0.01$$

b 720  

$$w_{omax} = 6.17 \text{ mm} \le \begin{cases} 7 \text{ mm for ship bottom plate} \\ 6 \text{ mm for ship deck plate} \end{cases}$$

282

For the stiffened-plate structure studied in the present paper, the welding-induced initial deflection satisfies the tolerance limit by ship classification societies or other regulatory bodies, confirming that the fabrication of the test structure was good enough.

#### 287 **7. Concluding remarks**

The aim of the paper was to obtain direct measurement databases of welding-induced initial deflections in a full-scale steel plate structure, and also to compare them with computational predictions. Based on the study, the following conclusions can be drawn.

- (1) A full-scale steel stiffened plate structure was designed and fabricated in a
  shipyard using exactly the same technology of welding as used in today's
  shipbuilding industry.
- (2) 3D scanner was used for measuring welding-induced initial deflections of
   plate panels as a non-contact method. It is confirmed that the 3D scanner is
   useful to measure the welding-induced initial deformations.

- (3) Three-dimensional thermo-elastic-plastic finite element method models were
   developed to predict welding-induced initial deformations of the structure. It
   is confirmed that the computational models predict the magnitude and shape
   welding-induced initial deflections of plate panels at a reasonable level of the
   accuracy.
- 303 (4) The database obtained in the paper will be useful for validating computational304 models developed by other engineers.

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#### 311 ORCID

- 312 Myung Su Yi. http://orcid.org/0000-0002-6984-5146
- 313 Dong Hun Lee. http://orcid.org/0000-0003-2829-0719
- 314 Hyun Ho Lee. http://orcid.org/0000-0001-7073-1069
- 315 Jeom Kee Paik. http://orcid.org/0000-0003-2956-9359
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Appendix: Measured welding-induced initial deformations of the test structure
 386



**Fig. A.1.** Measurement locations.

389

**Table A1.** Measured database of the initial deflections normalized by plate thickness

(a) Plate initial deflection for  $a = 0 \sim 3,150 \text{ mm}$  (z-direction)

Plate initial deflections		Longitudinal direction ( $a = 0 \sim 3,150 \text{ mm}$ )										
		0	350	700	1,050	1,400	1,750	2,100	2,450	2,800	3,150	
(	$w_0 / t_p$	)	L1	L2	L3	L4	L5	L6	L7	L8	L9	L10
	0	T1	-0.00033	0.01476	0.01891	0.02164	0.02286	0.02172	0.01834	0.01422	0.01532	0.00307
	120	T2	-0.00072	0.01097	0.01674	0.02024	0.02147	0.02052	0.01772	0.01376	0.01153	0.00519
-	240	T3	-0.00110	0.00904	0.01565	0.01918	0.02027	0.01946	0.01726	0.01409	0.01024	0.00616
(mm (	384	T4	-0.00154	0.01159	0.01678	0.01843	0.01899	0.01837	0.01727	0.01732	0.01689	0.00719
. 2,64(	528	T5	-0.00198	0.01561	0.01912	0.01856	0.01861	0.01812	0.01792	0.02134	0.02566	0.00792
~ 0 =	672	T6	-0.00238	0.01585	0.01932	0.01895	0.01915	0.01863	0.01825	0.02154	0.02663	0.00845
ion (b	816	T7	-0.00272	0.01179	0.01729	0.01966	0.02066	0.02001	0.01847	0.01802	0.01887	0.00879
direct	960	T8	-0.00301	0.00878	0.01694	0.02170	0.02354	0.02298	0.02056	0.01690	0.01272	0.00895
verse	1,104	T9	-0.00313	0.01316	0.02157	0.02583	0.02811	0.02817	0.02635	0.02338	0.01917	0.00895
Frans	1,248	T10	-0.00322	0.01858	0.02685	0.02964	0.03200	0.03274	0.03199	0.03102	0.02805	0.00881
	1,392	T11	-0.00322	0.01868	0.02698	0.02984	0.03222	0.03292	0.03211	0.03111	0.02827	0.00854
	1,536	T12	-0.00315	0.01331	0.02177	0.02612	0.02837	0.02832	0.02634	0.02330	0.01930	0.00814
	1,680	T13	-0.00305	0.00880	0.01685	0.02141	0.02300	0.02218	0.01956	0.01578	0.01154	0.00760

1,824	T14	-0.00275	0.01195	0.01675	0.01813	0.01839	0.01733	0.01562	0.01475	0.01485	0.00702
1,968	T15	-0.00242	0.01604	0.01779	0.01538	0.01416	0.01294	0.01234	0.01504	0.01991	0.00628
2,112	T16	-0.00202	0.01540	0.01631	0.01309	0.01124	0.00963	0.00897	0.01208	0.01804	0.00545
2,256	T17	-0.00157	0.01108	0.01414	0.01372	0.01258	0.01064	0.00867	0.00852	0.01051	0.00453
2,400	T18	-0.00112	0.01030	0.01773	0.02154	0.02233	0.02073	0.01738	0.01293	0.00803	0.00346
2,520	T19	-0.00073	0.01605	0.02597	0.03217	0.03474	0.03410	0.03063	0.02445	0.01567	0.00269
2,640	T20	-0.00033	0.02617	0.03901	0.04751	0.05223	0.05329	0.05072	0.04391	0.03108	0.00155

	Plate			]	Longitue	dinal dir	rection (	a = 3,13	50 ~ 6,3	<b>00 mm</b> )	)	
initia	l deflec	tions	3,150	3,500	3,850	4,200	4,550	4,900	5,250	5,600	5,950	6,300
(	$\left( w_0 / t_p \right)$	)	L10	L11	L12	L13	L14	L15	L16	L17	L18	L19
	0	T1	0.00307	0.00870	0.00175	0.00117	0.00145	0.00140	0.00104	0.00158	0.00860	0.00312
	120	T2	0.00519	0.00495	0.00126	0.00047	0.00018	0.00013	0.00036	0.00112	0.00487	0.00527
	240	Т3	0.00616	0.00367	0.00154	-0.00014	-0.00106	-0.00110	-0.00025	0.00140	0.00360	0.00626
	384	T4	0.00719	0.01029	0.00465	-0.00030	-0.00235	-0.00238	-0.00039	0.00455	0.01024	0.00729
	528	T5	0.00792	0.01900	0.00870	0.00043	-0.00250	-0.00252	0.00036	0.00863	0.01899	0.00803
	672	T6	0.00845	0.02001	0.00911	0.00106	-0.00164	-0.00166	0.00102	0.00908	0.02006	0.00856
m)	816	T7	0.00879	0.01253	0.00603	0.00186	0.00043	0.00042	0.00184	0.00603	0.01259	0.00891
540 m	960	T8	0.00895	0.00682	0.00563	0.00500	0.00473	0.00473	0.00501	0.00566	0.00688	0.00907
) ~ 2,0	1,104	Т9	0.00895	0.01373	0.01304	0.01227	0.01196	0.01198	0.01232	0.01312	0.01380	0.00907
) = q)	1,248	T10	0.00881	0.02277	0.02133	0.01898	0.01812	0.01815	0.01907	0.02146	0.02289	0.00892
ection (1	1,392	T11	0.00854	0.02279	0.02127	0.01892	0.01807	0.01811	0.01901	0.02141	0.02296	0.00865
se dire	1,536	T12	0.00814	0.01337	0.01237	0.01145	0.01114	0.01116	0.01152	0.01248	0.01351	0.00824
nsver	1,680	T13	0.00760	0.00494	0.00317	0.00209	0.00160	0.00162	0.00215	0.00325	0.00504	0.00769
Tra	1,824	T14	0.00702	0.00744	0.00030	-0.00457	-0.00663	-0.00661	-0.00451	0.00040	0.00753	0.00710
	1,968	T15	0.00628	0.01154	-0.00128	-0.01060	-0.01442	-0.01441	-0.01054	-0.00118	0.01164	0.00635
	2,112	T16	0.00545	0.00891	-0.00568	-0.01609	-0.02041	-0.02040	-0.01607	-0.00562	0.00899	0.00551
	2,256	T17	0.00453	0.00138	-0.00922	-0.01632	-0.01942	-0.01943	-0.01633	-0.00922	0.00142	0.00458
	2,400	T18	0.00346	0.00033	-0.00186	-0.00329	-0.00398	-0.00398	-0.00328	-0.00185	0.00034	0.00350
	2,520	T19	0.00269	0.00991	0.01351	0.01557	0.01645	0.01648	0.01564	0.01362	0.01000	0.00271
	2,640	T20	0.00155	0.02803	0.03830	0.04335	0.04547	0.04553	0.04354	0.03858	0.02830	0.00156

395 (b) Plate initial deflection for  $a = 3,150 \sim 6,300 \text{ mm} (z \text{-direction})$ 

	Plate		Longitudinal direction ( $a = 6,300 \sim 9,650 \text{ mm}$ )									
initia	l deflec	tions	6,300	6,650	7,000	7,350	7,700	8,050	8,400	8,750	9,100	9,450
(	$\left( w_0 / t_p \right)$	)	L19	L20	L21	L22	L23	L24	L25	L26	L27	L28
	0	T1	0.00312	0.01575	0.01519	0.01988	0.02379	0.02535	0.02444	0.02177	0.01510	-0.00034
	120	T2	0.00527	0.01196	0.01469	0.01919	0.02250	0.02387	0.02292	0.01949	0.01251	-0.00076
	240	Т3	0.00626	0.01069	0.01499	0.01866	0.02136	0.02260	0.02180	0.01828	0.01115	-0.00120
	384	T4	0.00729	0.01737	0.01817	0.01856	0.02014	0.02124	0.02106	0.01924	0.01247	-0.00161
	528	T5	0.00803	0.02612	0.02210	0.01904	0.01968	0.02067	0.02110	0.02132	0.01531	-0.00207
	672	T6	0.00856	0.02698	0.02213	0.01912	0.01983	0.02078	0.02106	0.02121	0.01551	-0.00248
m)	816	T7	0.00891	0.01910	0.01842	0.01903	0.02079	0.02172	0.02107	0.01882	0.01230	-0.00285
540 m	960	Т8	0.00907	0.01293	0.01722	0.02101	0.02357	0.02430	0.02265	0.01811	0.00995	-0.00320
) ~ 2,6	1,104	Т9	0.00907	0.01949	0.02385	0.02700	0.02901	0.02912	0.02696	0.02242	0.01267	-0.00330
(b = d	1,248	T10	0.00892	0.02844	0.03166	0.03286	0.03386	0.03334	0.03106	0.02744	0.01673	-0.00338
ection (ł	1,392	T11	0.00865	0.02858	0.03168	0.03289	0.03391	0.03339	0.03108	0.02746	0.01685	-0.00339
se dire	1,536	T12	0.00824	0.01945	0.02357	0.02668	0.02875	0.02891	0.02676	0.02225	0.01274	-0.00333
nsver	1,680	T13	0.00769	0.01159	0.01579	0.01953	0.02216	0.02305	0.02164	0.01738	0.00955	-0.00325
Tra	1,824	T14	0.00710	0.01491	0.01473	0.01556	0.01733	0.01860	0.01871	0.01741	0.01152	-0.00291
	1,968	T15	0.00635	0.01998	0.01508	0.01240	0.01317	0.01481	0.01659	0.01864	0.01439	-0.00255
	2,112	T16	0.00551	0.01805	0.01210	0.00905	0.00998	0.01211	0.01461	0.01743	0.01377	-0.00213
	2,256	T17	0.00458	0.01049	0.00849	0.00874	0.01096	0.01336	0.01507	0.01547	0.01083	-0.00166
	2,400	T18	0.00350	0.00808	0.01303	0.01758	0.02109	0.02290	0.02236	0.01881	0.01141	-0.00122
	2,520	T19	0.00271	0.01595	0.02487	0.03114	0.03462	0.03519	0.03247	0.02634	0.01671	-0.00077
	2,640	T20	0.00156	0.03174	0.04489	0.05176	0.05413	0.05256	0.04704	0.03804	0.02571	-0.00034

398 (c) Plate initial deflection for  $a = 6,300 \sim 9,650 \text{ mm}$  (z-direction)



**Fig. A.2.** Definition of stiffener's deflections.

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**Table A2.** Measured initial deflections of stiffeners normalized by stiffener thickness

406	(a) Initial deflection	n of the longitudinal stiff	ener (z-direction)

	Stiffener					Longit	udinal d	lirection	n ( a = 0	~ 3,150	mm)		
in	initial deflections			0	350	700	1,050	1,400	1,750	2,100	2,450	2,800	3,150
	$(w_0 / t_s)$			L1	L2	L3	L4	L5	L6	L7	L8	L9	L10
direction	(uu	240	Т3	0.00616	0.00367	0.00154	-0.00014	-0.00106	-0.00110	-0.00025	0.00140	0.00360	0.00626
	,640 r	960	Т8	0.00895	0.00682	0.00563	0.00500	0.00473	0.00473	0.00501	0.00566	0.00688	0.00907
sverse	$0 \sim 2$	1,680	T13	0.00760	0.00494	0.00317	0.00209	0.00160	0.00162	0.00215	0.00325	0.00504	0.00769
Tran (b =		2,400	T18	0.00346	0.00033	-0.00186	-0.00329	-0.00398	-0.00398	-0.00328	-0.00185	0.00034	0.00350

	S	tiffene	r		Ι	Longitud	linal dir	ection (	a = 3,15	50 ~ 6,3	00 mm )	)	
in	initial deflections $(w_{1}/t_{2})$			3,150	3,500	3,850	4,200	4,550	4,900	5,250	5,600	5,950	6,300
	(	$w_0 / t_s$ )	1	L10	L11	L12	L13	L14	L15	L16	L17	L18	L19
sverse direction $0 \sim 2,640 \text{ mm}$ )	(uu	240	T3	0.00616	0.00367	0.00154	-0.00014	-0.00106	-0.00110	-0.00025	0.00140	0.00360	0.00626
	,640 r	960	T8	0.00895	0.00682	0.00563	0.00500	0.00473	0.00473	0.00501	0.00566	0.00688	0.00907
	$0 \sim 2$	1,680	T13	0.00760	0.00494	0.00317	0.00209	0.00160	0.00162	0.00215	0.00325	0.00504	0.00769
Tran	= q)	2,400	T18	0.00346	0.00033	-0.00186	-0.00329	-0.00398	-0.00398	-0.00328	-0.00185	0.00034	0.00350

	Stiffener				Ι	Longitud	linal dir	ection (	a = 6,30	)0 ~ 9,6	50 mm )	)	
in	initial deflections $(w_{1}/t_{2})$			6,300	6,650	7,000	7,350	7,700	8,050	8,400	8,750	9,100	9,450
	(	$(w_0 / t_s)$		L19	L20	L21	L22	L23	L24	L25	L26	L27	L28
ction	(uu	240	Т3	0.00626	0.01069	0.01499	0.01866	0.02136	0.02260	0.02180	0.01828	0.01115	-0.00120
e direc	,640 n	960	Т8	0.00907	0.01293	0.01722	0.02101	0.02357	0.02430	0.02265	0.01811	0.00995	-0.00320
sverse	$0 \sim 2$	1,680	T13	0.00769	0.01159	0.01579	0.01953	0.02216	0.02305	0.02164	0.01738	0.00955	-0.00325
Tran: (b =		2,400	T18	0.00350	0.00808	0.01303	0.01758	0.02109	0.02290	0.02236	0.01881	0.01141	-0.00122

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# 416 (b) Initial deflection of the transverse stiffener (z-direction)

S	Stiffener				Trans	verse di	irection	( b = 0 ~	~ 1,248	mm )		
initial	l deflec	tions	0	120	240	384	528	672	816	960	1,104	1,248
(	$W_0 / t_s$ )		T1	T2	T3	T4	T5	T6	T7	Т8	Т9	T10
al direction ,650 mm)	0	L10	0.00307	0.00519	0.00616	0.00719	0.00792	0.00845	0.00879	0.00895	0.00895	0.00881
Longitudin: $(a = 0 \sim 9)$	120	L19	0.00312	0.00527	0.00626	0.00729	0.00803	0.00856	0.00891	0.00907	0.00907	0.00892

S	Stiffene	r			Transve	erse dire	ction ( ł	o = 1,39	2 ~ 2,64	0 mm )		
initia	initial deflections $(w_0 / t_s)$			1,536	1,680	1,824	1,968	2,112	2,256	2,400	2,520	2,640
(	$(w_0/t_s)$			T12	T13	T14	T15	T16	T17	T18	T19	T20
al direction ,650 mm)	0	L10	0.00854	0.00814	0.0076	0.00702	0.00628	0.00545	0.00453	0.00346	0.00269	0.00155
Longitudin: $(a = 0 \sim 9)$	120	L19	0.00865	0.00824	0.00769	0.0071	0.00635	0.00551	0.00458	0.0035	0.00271	0.00156

# 420421 (c) Sideway initial deflection of the longitudinal stiffener (y-direction)

	S	tiffene	r			Longi	tudinal o	direction	n ( a = 0	~ 3,150	) mm )		
side	ewa	y defle	ctions	0	350	700	1,050	1,400	1,750	2,100	2,450	2,800	3,150
	(	$w_0 / t_s$ )		L1	L2	L3	L4	L5	L6	L7	L8	L9	L10
ction	(uu	240	Т3	-0.00046	-0.00032	-0.00016	0.00016	0.00056	0.00087	0.00106	0.00128	0.00171	0.00429
direc	$,640 \mathrm{m}$	960	Т8	-0.00055	-0.00111	-0.00220	-0.00319	-0.00367	-0.00340	-0.00229	-0.00058	0.00110	0.00363
sverse	: 0 ~ 2,	1,680	T13	-0.00067	0.00018	0.00165	0.00316	0.00426	0.00465	0.00422	0.00311	0.00188	0.00307
Tran	= q)	2,400	T18	-0.00074	-0.00303	-0.00680	-0.01042	-0.01262	-0.01258	-0.00997	-0.00530	-0.00039	0.00289

	S	tiffene	r		I	Longitue	dinal dir	rection (	a = 3,1	50 ~ 6,3	00 mm	)	
sid	ewa	y defle	ctions	3,150	3,500	3,850	4,200	4,550	4,900	5,250	5,600	5,950	6,300
	(	$W_0 / t_s$ )		L10	L11	L12	L13	L14	L15	L16	L17	L18	L19
tion	(mn	240	Т3	0.00429	0.00424	0.00444	0.00525	0.00597	0.00598	0.00528	0.00448	0.00429	0.00438
e direc	,640 r	960	Т8	0.00363	0.00172	-0.00218	-0.00601	-0.00826	-0.00826	-0.00599	-0.00215	0.00179	0.00372
sverse	: 0 ~ 2,	1,680	T13	0.00307	0.00598	0.01081	0.01526	0.01784	0.01784	0.01528	0.01083	0.00602	0.00316
Tran (b =		2,400	T18	0.00289	-0.00552	-0.02028	-0.03395	-0.04184	-0.04184	-0.03394	-0.02024	-0.00545	0.00295

	S	tiffener	r		]	Longitud	dinal dir	rection (	a = 6,3	00 ~ 9,6	50 mm	)	
sid	ewa	y defle	ctions	6,300	6,650	7,000	7,350	7,700	8,050	8,400	8,750	9,100	9,450
	(	$w_0/t_s$ )		L19	L20	L21	L22	L23	L24	L25	L26	L27	L28
ction	(mn	240	Т3	0.00438	0.00180	0.00143	0.00128	0.00113	0.00081	0.00038	-0.00001	-0.00027	-0.00055
e direc	,640 r	960	Т8	0.00372	0.00116	-0.00051	-0.00219	-0.00326	-0.00350	-0.00300	-0.00205	-0.00108	-0.00063
sverse	$0\sim 2,$	1,680	T13	0.00316	0.00197	0.00326	0.00441	0.00486	0.00443	0.00327	0.00169	0.00016	-0.00074
Tran	= q)	2,400	T18	0.00295	-0.00041	-0.00536	-0.01002	-0.01257	-0.01253	-0.01030	-0.00677	-0.00312	-0.00080

	· /									· · ·		,		
	Stiffener				Transverse direction ( $a = 0 \sim 2,640 \text{ mm}$ )									
sideway deflections					0	120	240	384	528	672	816	960	1,104	1,248
	$(w_0 / t_s)$				T1	T2	T3	T4	T5	T6	T7	T8	Т9	T10
Longitudinal direction	al direction	,650 mm)	3150	L10	-0.01591	-0.01593	-0.01595	-0.01598	-0.01600	-0.01602	-0.01604	-0.01605	-0.01605	-0.01604
	Longitudin	$(a = 0 \sim 9,$	6300	L19	-0.04533	-0.04528	-0.04523	-0.04516	-0.04509	-0.04503	-0.04497	-0.04491	-0.04487	-0.04484

427 (d) Sideway initial deflection of the transverse stiffener (x-direction)

	S	tiffener	r	Transverse direction ( $a = 0 \sim 2,640 \text{ mm}$ )									
sid	ewa	y defle	ctions	1,392	1,536	1,680	1,824	1,968	2,112	2,256	2,400	2,520	2,640
	(	$w_0 / t_s$ )		T11	T12	T13	T14	T15	T16	T17	T18	T19	T20
al direction	$(a = 0 \sim 9,650 \text{ mm})$	3150	L10	-0.01603	-0.01601	-0.01598	-0.01595	-0.01591	-0.01585	-0.01579	-0.01572	-0.01568	-0.01563
Longitudina		6300	L19	-0.04481	-0.04479	-0.04478	-0.04478	-0.04479	-0.04481	-0.04484	-0.04487	-0.04490	-0.04493